BDD-Based Algorithms for Packet Classification

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Abstract—Packet classifiers are the building blocks of modern networking. A classifier determines the action to take on a packet by matching its header against a set of rules. Efficient classification is achieved by using associative memory to perform the match operation in one clock cycle. This requires compressing large rule sets to fit in the small associative memory space available in modern network switches. Failure to do so leads to increased infrastructure cost and reduced performance. We propose two symbolic rule set compression algorithms based on binary decision diagrams. Following McGeer and Yalagandula, we formalize the problem as that of obtaining a sequential cover of the rule set. We develop a simple BDD-based algorithm for computing sequential covers, which significantly outperforms state of the art algorithms in terms of compression ratio—a surprising result that highlights the unexplored potential of symbolic techniques in packet classification. Despite this improvement, very large industrial classifiers are still beyond reach. We decompose such classifiers into a pipeline of smaller classifiers over subsets of packet header fields. We then compress each classifier using the sequential cover technique. Our algorithm is able to compress industrial rule sets with hundreds of thousands of rules to readily fit in the memory of network switches.

I. INTRODUCTION

Modern datacenter, corporate, and telecom networks have evolved beyond their traditional role as communication substrate providing end-host connectivity. Nowadays these networks implement a rich set of functions, including firewalls, routing, load balancing, and service chaining, to name a few. Inside network switches, these functions are implemented as packet classifiers, which determine the next action to perform on the packet (e.g., drop or forward) by matching its headers against a set of rules, e.g., "Drop UDP packets sent from hosts in the 172.16.*.* IP subnet with destination port numbers in the 554–680 range." Moreover, multi-terabit-per-second packet processing rates, supported in modern network switches, require packet classification to complete in a short and constant time. To this end, switches are equipped with ternary content-addressable memories (TCAMs), also known as associative memories, capable of matching a packet against multiple rules in a single clock cycle.

Due to their high cost and power consumption, TCAMs remain a limited resource. Current high-end switches are equipped with thousands to tens of thousands of TCAM entries. In contrast, real-world packet classifiers may consist of hundreds of thousands rules. Whenever the rule set does not fit in the TCAM of a single switch, the network administrator is left with two options: (1) partition the rule set across multiple switches, dramatically raising the cost and complexity of network management, or (2) sacrifice performance by moving a subset of rules to conventional memory.

Rule set compression mitigates the problem by computing a smaller rule set equivalent to the original classifier. It can be used to fit a large classifier in the TCAM of a single switch or to enable integrated functionality by configuring a single switch with multiple classifiers.

Rule set compression algorithms represent rules as hypercubes in the multidimensional space of packet headers, seeking to cover the entire classifier with as few cubes as possible. Since computing an optimal solution to this problem is NP-hard [1], greedy heuristics are employed to reduce the search space. Ultimately, finding a small cover within a reasonable time frame depends on the ability of the algorithm to efficiently compute unions and intersections of cubes.

Existing algorithms represent cubes explicitly. We argue that significant speedup can be achieved by symbolically representing and manipulating sets of cubes as Binary Decision Diagrams (BDDs) [2]. In fact, simply by compiling the rule set to a BDD we obtain a compact representation of all its cubes. Furthermore, BDDs allow efficiently extracting prime implicants, i.e., cubes that are not contained within any other cube of the rule set. Based on this observation, we develop two BDD-based algorithms for rule set compression. Following McGeer and Yalagandula [3], we formulate the compression problem as that of computing sequential cover of the rule set. We propose a BDD-based algorithm for computing sequential cover. Our algorithm outperforms state of the art rule set compression algorithms, e.g., where the best known algorithm achieves 50% compression ratio, we achieve 10x compression.

Next we apply the same approach to three very large real-world classifiers with hundreds of thousands rules. To the best of our knowledge, these are the largest rule sets reported in the literature. We observe that on these rule sets, our algorithm still does not achieve satisfactory compression ratio. We therefore propose a new compression algorithm that decomposes the rule set into a pipeline of packet classifiers, where each classifier matches on a subset of packet header fields and computes a tag used as input to the next classifier. Our decomposition is based on the BDD-based functional decomposition technique by Lai et al. [4]. We compress each classifier by computing its sequential cover, as above.

We apply this algorithm to our real-world classifiers and show that it achieves two to four orders of magnitude compression on these classifiers, reducing them to readily fit into the TCAM table space of modern switches.

Our main contribution is a pair of algorithms that significantly improve the state of the art in packet classification—a problem of great practical importance that has attracted a lot
of prior research in the networking community. To the best of our knowledge, this work is the first to apply two well-known logic minimization techniques—symbolic prime cover computation and functional decomposition—in this space. As such, we hope that it will stimulate further research on symbolic algorithms for packet classification.

II. BACKGROUND

**Boolean logic** Let \( z_1, \ldots, z_l \) be a set of Boolean variables. A **literal** is a Boolean variable \( z_i \) or its negation \( \neg z_i \). A **cube** is a conjunction of literals, e.g., \( z_1 \neg z_2 z_3 \). We denote \( \{ z_1, \ldots, z_j \} \) the restriction of cube \( c \) on variables \( \{ z_i_1, \ldots, z_i_j \} \), obtained by eliminating all literals over other variables. A cube \( c \) is an **implicant** of a boolean function \( g : B^j \rightarrow B \) iff \( c \Rightarrow g(\hat{z}_1, \ldots, \hat{z}_l) \); \( c \) is a **prime implicant** if it cannot be reduced, i.e., the removal of any literal from \( c \) results in a non-implicant.

**Packet classification** A packet **header** is a fixed-size bit vector \( X = (x_1, \ldots, x_n) \), where a Boolean variable \( x_i \) corresponds to the \( i \)th bit of the header. Individual header bits are grouped into **fields**, which represent source and destination IP addresses of the packet, port numbers, etc. : \( X = (X_1, \ldots, X_l) \), where bitvector \( X_j \) is the \( j \)th field of the header. A packet **classifier** \( f : B^n \rightarrow A \) maps a header into one of a finite set of actions \( A \), where \( B = \{0, 1\} \). To encode classifiers to BDDs, we represent \( f \) as a function \( F : B^n \times A \rightarrow B \) such that \( F(X, Y) = T \) \( \equiv f(X) = Y \). We assume that \( A \) is encoded using Boolean variables, for example \( A = \{ \text{ACCEPT}, \text{DENY} \} \) is encoded using a single Boolean.

Classifiers are represented as ordered lists of rules of the form \( R = ((m_1, a_1), \ldots, (m_k, a_k)) \), where \( m_j : B^n \rightarrow A \) is a match function that identifies a subset of the header space and \( a_j \in A \) is the action to perform on the packet when its header belongs to this subset (note that \( a_j \) are not required to be distinct). The corresponding classifier \( F_R \) picks the first rule that matches the header:

\[
F_R(X, Y) = m_1(X) \land (Y = a_1) \lor m_2(X) \land (Y = a_2) \ldots \lor m_k(X) \land (Y = a_k) \tag{1}
\]

To make sure that \( F_R \) defines a unique action for any header, the final rule \( (m_k, a_k) \) is a catch-all rule that matches all headers: \( m_k(X) \equiv T \).

**Rule languages** Network switches equipped with TCAMs are programmed using rules expressed in ternary form. Consider a header field \( X_j = (z_1, \ldots, z_p) \). A **ternary constraint** fixes a subset of bits in \( X_j \), leaving other bits unconstrained, i.e., it is a cube over \( X_j \). **Prefix constraints**, frequently used in practice, are a special case of ternary constraints, that fix a prefix of the bit vector. A **ternary rule** is a rule whose match function is a conjunction of ternary constraints, one for each field \( X_j \), \( j \in [1, l] \). Equivalently, a ternary rule is a cube over \( X \).

**Example 1:** Figure 1(a) shows an example ternary rule set where \( x_i \) are header variables and \( y \) is the action variable.

In writing network policies, network administrators often use **range constraints**. A **range constraint** \( c_1 \leq X_j \leq c_2 \) interprets field \( X_j \) as an integer value stored using logarithmic encoding and requires this value to be in the range \( [c_1, c_2] \). Rules with range constraints can be decomposed into multiple ternary rules by rewriting each range constraint as a disjunction of ternary constraints and taking a Cartesian product across all range constraints in the rule.

Modern network management software supports even richer policy languages that allow various Boolean combinations of range and ternary constraints. Such general rules can be decomposed into ternary rules by flattening their Boolean structure to Disjunctive Normal Form. Such expansion can be too expensive in practice and therefore should be avoided.

**BDDs** A **BDD** [2] is a compressed canonical representation of the binary decision tree of a Boolean function in the form of a directed acyclic graph. Figure 1(b) shows a BDD of the classifier specified in Figure 1(a).

**Problem statement** The rule set compression problem can be defined as follows: given a rule set \( R \), written using any rule language, compute a minimal ternary rule set \( R' \) such that \( F_R \equiv F_{R'} \). Computing an optimal solution is NP-hard [1]; therefore in practice we aim to achieve the best possible compression within a reasonable time frame.

III. COMPRESSION VIA SEQUENTIAL COVER

McGeer and Yalagandula [3] introduced the notion of **sequential cover** for rule set compression. A sequential cover of a classifier \( F(X, Y) \) is a set of cubes \( p_j \), \( j \in [1, u] \) over variables \( X \) and \( Y \) such that (1) \( p_j \) cover the entire classifier: \( F(X, Y) \Rightarrow \bigvee_{j \in [1, u]} p_j \); and (2) each \( p_j \) is a prime implicant of function \( F(X, Y) \lor \bigvee_{j < j} p_j(X) \). The second condition states that each rule must only agree with \( F \) on headers not covered by previous rules; the rest of the header space is the don’t care set where the rule can disagree with \( F \). Note that sequential
TABLE I: CERNET rule sets.

<table>
<thead>
<tr>
<th>Name</th>
<th>R</th>
<th>#ExpR</th>
<th>#Nodes</th>
<th>MDTC</th>
<th>Flint</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Rules</td>
<td>Ratio</td>
<td>Time(s)</td>
<td>Rules</td>
<td>Ratio</td>
</tr>
<tr>
<td>cernet1</td>
<td>21</td>
<td>21</td>
<td>42</td>
<td>6</td>
<td>0.59</td>
</tr>
<tr>
<td>cernet2</td>
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<td>165</td>
<td>37</td>
<td>0.95</td>
<td>0.00</td>
</tr>
<tr>
<td>cernet3</td>
<td>44</td>
<td>44</td>
<td>19</td>
<td>0.43</td>
<td>0.00</td>
</tr>
<tr>
<td>cernet4</td>
<td>52</td>
<td>52</td>
<td>112</td>
<td>1.00</td>
<td>0.00</td>
</tr>
<tr>
<td>cernet5</td>
<td>175</td>
<td>175</td>
<td>720</td>
<td>1.95</td>
<td>0.03</td>
</tr>
<tr>
<td>cernet6</td>
<td>664</td>
<td>664</td>
<td>686</td>
<td>0.78</td>
<td>0.05</td>
</tr>
<tr>
<td>cernet7</td>
<td>943</td>
<td>5161</td>
<td>881</td>
<td>0.93</td>
<td>0.14</td>
</tr>
<tr>
<td>cernet8</td>
<td>1491</td>
<td>1564</td>
<td>1664</td>
<td>1.01</td>
<td>0.35</td>
</tr>
</tbody>
</table>

TABLE II: Synthetic benchmarks (reports means across all rule sets in each benchmark).

<table>
<thead>
<tr>
<th>Name</th>
<th>R</th>
<th>#ExpR</th>
<th>#Nodes</th>
<th>MDTC</th>
<th>Flint</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Rules</td>
<td>Ratio</td>
<td>Time(s)</td>
<td>Rules</td>
<td>Ratio</td>
</tr>
<tr>
<td>acl-small</td>
<td>936</td>
<td>1305</td>
<td>1753</td>
<td>100</td>
<td>0.08</td>
</tr>
<tr>
<td>acl-large</td>
<td>9125</td>
<td>1232K</td>
<td>15.97K</td>
<td>1385</td>
<td>0.11</td>
</tr>
<tr>
<td>fw-small</td>
<td>847</td>
<td>3382</td>
<td>6474</td>
<td>1311</td>
<td>0.39</td>
</tr>
<tr>
<td>fw-large</td>
<td>8737</td>
<td>35.71K</td>
<td>14.64K</td>
<td>6108</td>
<td>0.17</td>
</tr>
<tr>
<td>ipc-small</td>
<td>916</td>
<td>1343</td>
<td>8360</td>
<td>566</td>
<td>0.42</td>
</tr>
<tr>
<td>ipc-large</td>
<td>8623</td>
<td>11.86K</td>
<td>12.91K</td>
<td>981</td>
<td>0.08</td>
</tr>
</tbody>
</table>

cover is similar to the classical notion of *prime cover*, where all implications must agree with $F$.

Each $p_j$ in the sequential cover of $F$ can be interpreted to a rule $r'_j = (m_j', a'_j')$, where $m_j' = p_j \setminus X$ and $a'_j$ is obtained by extracting the action from $p_j \setminus X$. The resulting rule set $R' = ((m_j', a'_j), \ldots, (m_u', a'_u))$ is equivalent to $R$. A minimal rule set is an optimal solution to the rule set compression problem.

Example 2: Figure 1(c) shows a sequential cover of the classifier in Figure 1(a). Note that the last rule $(* * * * * 0)$ is not an implication of the classifier, since not all assignments of $x_1 \ldots x_5$ map to action 0. However, it is an implication of the classifier with the header space covered by previous rules added to its don’t care set, since all assignments of $x_1 \ldots x_5$ not covered by previous rules map to 0.

Algorithm 1 shows our BDD-based algorithm for computing a sequential cover. It takes a packet classifier $F$ and returns a subset $F'$ of $F$ not covered by the implications computed so far, and a superset $F''$ that includes the don’t care set covered by the previous implications. Sets $F, F' + F''$ are represented as BDDs and all operations on them are performed in the BDD form. The main loop of the algorithm computes a single new implication on every iteration by first extracting a largest cube (i.e., a cube with the smallest number of literals) from $F''$, which corresponds to a shortest path from the root to a leaf of the BDD. It then extends this cube to a prime implicant of $F' + F''$ by greedily removing literals from the cube so that the resulting cube is still in $F''$. Note that the algorithm is not guaranteed to produce a minimal sequential cover.

Performance We implemented Algorithm 1 in a tool called Flint using the CUDD BDD library [5]. We encode packet classifier $F_i$ into a BDD using formula 1. We use the group sifting [6] dynamic variable reordering heuristic, grouping variables that belong to the same field, to reduce the size of the resulting BDD. Due to the sensitive nature of real-world rule sets, very few of them are publicly available. We therefore use a mix of synthetic and real-world benchmarks in our evaluation. First, we use two datasets from [7]. The first of these datasets consists of 8 classifiers extracted from the CERNET network. The second dataset consists of 12 synthetic access control list (ACL) rule sets generated using the ClassBench tool [8]. We generate 5 additional synthetic datasets using ClassBench. These datasets fall into three categories: ACL, firewall (FW), and IP Chain (IPC). Each dataset consists of 20 rule sets. The header space in all rule sets consists of 5 fields and 104 bits. Table I compares Flint against MDTC [7], the most efficient rule set compression algorithm reported in the literature—on the CERNET dataset. It shows the size of the original rule set (Rules) and the expanded rule set obtained by decomposing range constraints into ternary constraints (ExpRules), the number of nodes in the BDD encoding of the classifier (Nodes), the compressed rule set size, compression ratio, and the run time of MDTC (based on [7]) and Flint.

As can be seen from the table, Flint improves the average compression ratio of MDTC by 21% on average on these rule sets. Table II reports results for synthetic benchmarks. For space reasons, we report mean values across all rule sets in each benchmark. The first row (‘acl-small’) shows results for the synthetic dataset from [7]. Flint dramatically outperforms MDTC on this dataset, achieving 13x compression on average, while Zhu et al. report 0.45 mean compression ratio for MDTC. The remaining rows show results for the 5 new synthetic datasets. Flint achieves over 2x compression in all cases and 5x-13x compression on the large datasets with > 8000 rules. Next, we apply Flint to three very large real-world customer rule sets with 70K, 599, and 1952 complex rules. Many of these rules have complex Boolean structure, so that their expanded representation, had we constructed it explicitly, would contain 276K, 64467K, and 194660K rules respectively. The header space in these rule sets consists of 9 fields and 366 bits. Flint compressed the first rule set into 3636 ternary rules; however on the two other rule sets we interrupted Flint after generating 200K rules. Clearly, a more efficient compression technique is required to handle such rule sets. We develop such a technique in the next section.

IV. COMPRESSION VIA FUNCTIONAL DECOMPOSITION

The following example illustrates the main source of explosion in the number of rules in the real-world rule sets. Consider a rule $(m, a)$, where $m$ is of the form $m_{X_1} \land m_{X_2}$, where $m_{X_1}$ and $m_{X_2}$ are arbitrary constraints over header fields $X_1$ and $X_2$. Assume that $m_{X_1}$ and $m_{X_2}$ can be decomposed into $i$ and $j$ cubes respectively. In this case, an optimal ternary encoding of rule $(m, a)$ may require up to $i \times j$ ternary rules. Alternatively, it can be decomposed into a sequence of two classifiers that check that header $X_1$ is in $m_{X_1}$ and $X_2$ is in $m_{X_2}$ respectively. This requires a total of $i + j$ rules. Furthermore, TCAM tables matching individual header fields are narrower, and hence require less TCAM memory, than the monolithic table. This optimization is compatible with modern network switches, which support both pipelined classifiers and configurable-width TCAMs [9].

In general, we would like to decompose a classifier $f : B^n \rightarrow A$ into a sequence of classifiers $f_i, i \in [1, l]$ where $f_i$ matches on a single header field $X_i$ and returns a tag.
Algorithm 2 Decompose classifier \( f \) into \( f_1, \ldots, f_t \)

1: function \textsc{DecomposeClassifier}(\( f \))
2: \( \gamma \leftarrow f \)
3: for \( i = 1 \) to \( t - 1 \) do
4: \( (f_i, \gamma) \leftarrow \textsc{Decompose}(g, X_i) \)
5: \( f_i \leftarrow g \)
6: return \( (f_1, \ldots, f_t) \)

TABLE III: Large real-world rule sets.

<table>
<thead>
<tr>
<th>Name</th>
<th>FID</th>
<th>#ExpR</th>
<th>#Nodes</th>
<th>Flint (rules)</th>
<th>Flint-DC</th>
</tr>
</thead>
<tbody>
<tr>
<td>real-world1</td>
<td>70.26K</td>
<td>275.99K</td>
<td>68.50</td>
<td>3636</td>
<td>2.60M</td>
</tr>
<tr>
<td>real-world2</td>
<td>599</td>
<td>64667.64K</td>
<td>171.60K</td>
<td>10.71K</td>
<td>0.00179</td>
</tr>
<tr>
<td>real-world3</td>
<td>1952</td>
<td>194660.96K</td>
<td>282.68K</td>
<td>-</td>
<td>28.03K</td>
</tr>
</tbody>
</table>

T_i used as input to the next classifier: \( f(X_1, \ldots, X_i) \) = \( f_i(f_{i-1}(\ldots f_2(f_1(X_1), X_2), \ldots), X_i) \).

Example 3: Figure 1(d) shows a decomposition of the classifier in Figure 1(a) into a sequence of two classifiers. The first classifier summarizes the values of variables \( x_1, x_2 \) using tag \( t \), which is passed as input to the second classifier.

We perform the decomposition iteratively, one field at a time, as shown in Algorithm 2. The main building block of the algorithm is the \textsc{Decompose} procedure that decomposes a function \( g(Z_1, Z_2) \) into a pair of functions \( (g_1, g_2) \) such that \( g(Z_1, Z_2) = g_2(g_1(Z_2), Z_2) \). Notice that this is exactly the \textit{functional decomposition} operation, thoroughly studied in logic synthesis [10]. We use a classical BDD-based functional decomposition algorithm by Lai et al. [4], outlined below.

Consider BDD representation \( G(Z_1, Z_2, W) \) of function \( g \) (variables \( W \) encode the output of \( g \)), ordered with variables \( Z_1 \) on top. Consider the cut of the graph below variables \( Z_1 \) and the set of boundary nodes \( v_1, \ldots, v_j \), located below the cut that have incoming edges from nodes above the cut. Figure 1(b) shows an example cut with boundary nodes \( v_1 \) and \( v_2 \). An assignment of \( Z_1 \) corresponds to a path from the root of the BDD to some nodes \( v_i \). Assignments that lead to the same \( v_i \) are indistinguishable to \( G \) and can be encoded using one tag. Conversely, due to the canonicity of BDGs, assignments that lead to different \( v_i \) are not equivalent and are encoded with distinct tags. Thus, we have partitioned valuations of \( Z_1 \) into \( j \) equivalence classes. We denote \( DD(v_i) \) a subgraph of \( G \) that consists of all paths from the root to \( v_i \). Converting \( DD(v_i) \) into canonical form and replacing \( v_i \) by terminal node \( T \), we obtain a BDD for the \( i \)th equivalence class.

We introduce fresh variables \( T, |T| = \lceil \log(j) \rceil \), to encode the \( j \) equivalence classes, and add constraints to \( G \) to compute the value of \( T \): \( G^j([Z_1, T, Z_2, W]) = G(Z_1, Z_2, W) \land \bigwedge_{i \in [1, j]}[DD(v_i) \Rightarrow (T = i)] \). We finally obtain the decomposition of \( G_1(Z_1, T) = \exists Z_2, W. G^j(Z_1, T, Z_2, W) \) and \( G_2(T, Z_2, W) = \exists Z_1, G^j(Z_1, T, Z_2, W) \), where \( G_1 \) computes the tag that encodes the equivalence class of variables \( Z_1 \), whereas \( G_2 \) evaluates the original function \( G \), using the equivalence class of \( Z_1 \) instead of its concrete value. The final step of our compression procedure, after computing \( f_1, \ldots, f_t \), is to encode each \( f_i \) into ternary rules using Algorithm 1.

Performance We applied the decomposition algorithm (Flint-DC) to the three real-world benchmarks. We decompose fields in the order in which they appear in the BDD encoding of the classifier, i.e., the order produced by group sift. Flint-DC produces compact ternary rule sets in all three cases (Table III). The biggest generated rule set contains 28K rules, which fits readily in the TCAM of modern switches [9]. Due to the lack of space, we do not report results for smaller rule sets from Section 3, where Flint-DC performs on a par with Flint. This indicates that functional decomposition works best for large rule sets. The following observation explains the effectiveness of Flint-DC on real-world rule sets. The algorithm depends on the ability to factor the set of values of a field into few equivalence classes, one for each boundary node between BDD layers. While some BDD layers in our rule sets have many nodes, boundary layers are always very thin. For example, in our largest rule set, only 6 bits per field were required on average to encode equivalence classes.

V. RELATED WORK

There exists a body of research on packet classification. See [8], [11]–[13] for a sample of work in this area. TCAM-based rule set compression is a special case of the problem, where the resulting classifier is encoded using ternary rules. Previous approaches represent sets of rules using lists [14]–[17] or trees [7], [18]. We show that a BDD-based representation allows computing more compact rule sets efficiently. Norige et al. [19] compile classifiers to BDD, but then decompile the BDD back into a tree or list representation to perform compression. In contrast, our algorithms are fully symbolic, i.e., operate on the BDD representation only. Prakash et al. [20] use BDGs as intermediate representation in converting packet classifiers to circuits. Smolka et al. [21] introduce a variant of BDGs, Forwarding Decision Diagrams, as an intermediate representation for compiling a high-level network programming language into OpenFlow. They extract cubes from FDDs via path enumeration. In contrast, Flint generates fewer larger cubes by generalizing them to prime implicants.

Meiners et al. compile packet classifiers to FDDs and slice them into a series of smaller classifiers. The algorithms they use to decompose and compress classifiers differ from ours. For example, they construct a separate FDD for each boundary node and concatenate these FDDs to obtain a classifier. In contrast, Flint compiles each classifier in the decomposition into a monolithic BDD and applies prime decomposition to it.

The notion of sequential cover for rule set compression was introduced in [3]. We propose an efficient BDD-based method of computing sequential cover. Chang et al. [22] proposed an optimized encoding of range constraints into ternary constraints. This work is complementary to ours and can potentially be used to replace the simple encoding we use.

VI. CONCLUSION

We developed two algorithms that significantly improve the state of the art in TCAM-based packet classification. While most previous solutions rely on specialized data structures and algorithms, we reduce the problem to standard problems in logic minimization and solve it using symbolic logic minimization techniques.
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